

# A METHODOLOGY FOR THE SIMPLIFICATION OF TABULAR DESIGNS IN MODEL-BASED DEVELOPMENT

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- ▷ Introduction
- ▷ Methodology
- ▷ Industrial Case Studies
- ▷ Conclusions

- Model-Based Development (MBD) is increasingly used for embedded control software
- Complex decision logic in Simulink is often implemented with *Stateflow truth tables*<sup>1</sup>
- Automotive partner has flagged some as particularly problematic
  - Hard to understand, test, and trace to requirements
  - ISO 26262 ASIL D stresses low complexity, MC/DC testing, unambiguous language constructs
- ▶ Thus, more effective tabular constructs and reliable refactoring techniques are needed

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<sup>1</sup>Classically known as *decision tables*

## Stateflow truth table

#	Conditions	Decisions			
		D <sub>1</sub>	D <sub>2</sub>	D <sub>3</sub>	D <sub>4</sub>
1	Condition <sub>1</sub>	T	T	T	-
2	Condition <sub>2</sub>	T	-	F	-
3	Condition <sub>3</sub>	T	T	-	-
	Actions	1	2	3	4

#	Actions
1	Action <sub>1</sub>
2	Action <sub>2</sub>
3	Action <sub>3</sub>
4	Action <sub>4</sub>

## Tabular Expressions

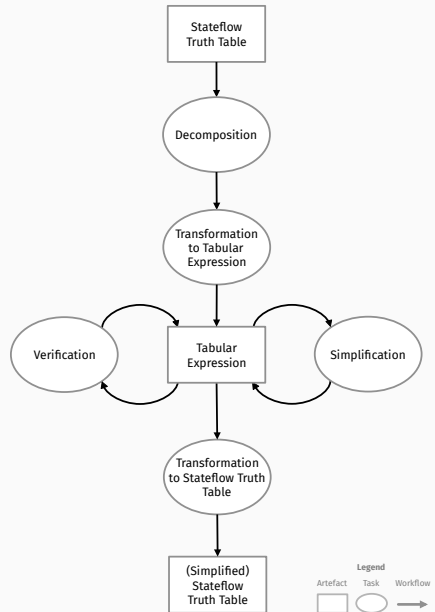
### Horizontal Condition Table (HCT)

Conditions		Result
		Var
Condition <sub>1</sub>	Condition <sub>2</sub>	Result <sub>1</sub>
	¬Condition <sub>2</sub>	Result <sub>2</sub>
¬Condition <sub>1</sub>		Result <sub>3</sub>

- Diagnostic tools do not check disjointness
- Implicit left-to-right semantics
- Completeness commonly forced with *else* catch-all case
- Non-Boolean conditions expressed unintuitively
- Readability does not scale well

- Disjointness required
- No prescribed row evaluation order
- Completeness is explicit
- More intuitive and concise syntax
- Easily readable and traceable to requirements

- Thus, we leverage the use of tabular expressions to remedy the deficiencies of Stateflow truth tables
- Guided refactoring is facilitated as logical simplifications are easier to detect and apply
- Heuristics were designed to be an easy-to-follow process of performing guided refactoring



# AUTOMOTIVE CASE STUDY 1

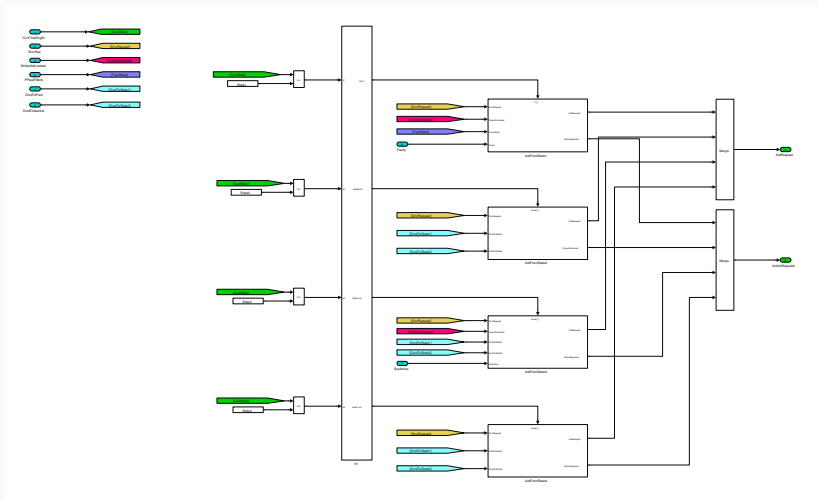


Figure 1: Subsystem for driver request arbitration

# ORIGINAL STATEFLOW TRUTH TABLE

#	Conditions	Decisions										
		D <sub>1</sub>	D <sub>2</sub>	D <sub>3</sub>	D <sub>4</sub>	D <sub>5</sub>	D <sub>6</sub>	D <sub>7</sub>	D <sub>8</sub>	D <sub>9</sub>	D <sub>10</sub>	D <sub>11</sub>
1	$eDrvrRequest == cState_1$	T	F	F	F	F	F	F	F	F	F	-
2	$eDrvrRequest == cState_2$	F	T	F	F	T	F	F	T	F	F	-
3	$eDrvrRequest == cState_3$	F	F	T	F	F	T	F	F	T	F	-
4	$eDrvrRequest == cState_4$	F	F	F	T	F	F	T	F	F	T	-
5	$bCmpntUnlocked$	-	T	T	T	-	-	-	-	-	-	-
6	$bFaulty$	-	F	F	F	T	T	T	-	-	-	-
	Actions	1	2	3	4	5	5	5	5	5	5	1

#	Actions
1	$eArbRequest=cState_1; bActionRequired=false$
2	$eArbRequest=cState_2; bActionRequired=false$
3	$eArbRequest=cState_3; bActionRequired=false$
4	$eArbRequest=cState_4; bActionRequired=false$
5	$eArbRequest=cState_1; bActionRequired=true$

Table 1: Driver request arbitration from  $cState_1$

# DECOMPOSITION

- If the table computes **multiple** outputs, decompose into multiple tables each computing a **single** output
  - Increases modularity, requirements traceability, greater reductions during simplification

#	Conditions	Decisions										
		D <sub>1</sub>	D <sub>2</sub>	D <sub>3</sub>	D <sub>4</sub>	D <sub>5</sub>	D <sub>6</sub>	D <sub>7</sub>	D <sub>8</sub>	D <sub>9</sub>	D <sub>10</sub>	D <sub>11</sub>
1	$eDrvrRequest == cState_1$	T	F	F	F	F	F	F	F	F	F	-
2	$eDrvrRequest == cState_2$	F	T	F	F	T	F	F	T	F	F	-
3	$eDrvrRequest == cState_3$	F	F	T	F	F	T	F	F	T	F	-
4	$eDrvrRequest == cState_4$	F	F	F	T	F	F	T	F	F	T	-
5	$bCmpntUnlocked$	-	T	T	T	-	-	-	-	-	-	-
6	$bFaulty$	-	F	F	F	T	T	T	-	-	-	-
	Actions	1	2	3	4	5	5	5	5	5	5	1

#	Conditions	Decisions											
		D <sub>1</sub>	D <sub>2</sub>	D <sub>3</sub>	D <sub>4</sub>	D <sub>5</sub>	D <sub>6</sub>	D <sub>7</sub>	D <sub>8</sub>	D <sub>9</sub>	D <sub>10</sub>	D <sub>11</sub>	
1	$eDrvrRequest == cState_1$	T	F	F	F	F	F	F	F	F	F	F	-
2	$eDrvrRequest == cState_2$	F	T	F	F	T	F	F	T	F	F	F	-
3	$eDrvrRequest == cState_3$	F	F	T	F	F	T	F	F	T	F	T	-
4	$eDrvrRequest == cState_4$	F	F	F	T	F	F	T	F	F	F	T	-
5	$bCmpntUnlocked$	-	T	T	T	-	-	-	-	-	-	-	-
6	$bFaulty$	-	F	F	F	T	T	T	-	-	-	-	-
	Actions	1	2	3	4	1	1	1	1	1	1	1	1

#	Actions
1	$eArbRequest=cState_1; bActionRequired=false$
2	$eArbRequest=cState_2; bActionRequired=false$
3	$eArbRequest=cState_3; bActionRequired=false$
4	$eArbRequest=cState_4; bActionRequired=false$
5	$eArbRequest=cState_1; bActionRequired=true$

(a) Original

#	Actions
1	$eArbRequest=cState_1$
2	$eArbRequest=cState_2$
3	$eArbRequest=cState_3$
4	$eArbRequest=cState_4$

(b) Decomposed



# STATEFLOW TRUTH TABLE → HCT

1. Augment decisions with conditions and actions
2. Transpose
3. Group related conditions
4. Ensure disjointness and completeness
5. Formatting

#	Conditions	Decisions										
		D <sub>1</sub>	D <sub>2</sub>	D <sub>3</sub>	D <sub>4</sub>	D <sub>5</sub>	D <sub>6</sub>	D <sub>7</sub>	D <sub>8</sub>	D <sub>9</sub>	D <sub>10</sub>	D <sub>11</sub>
1	$eDrvRequest == cState_1$	T	F	F	F	F	F	F	F	F	F	-
2	$eDrvRequest == cState_2$	F	T	F	F	T	F	F	T	F	F	-
3	$eDrvRequest == cState_3$	F	F	T	F	F	T	F	F	T	F	-
4	$eDrvRequest == cState_4$	F	F	F	T	F	F	T	F	F	T	-
5	$bCmpntUnlocked$	-	T	T	T	-	-	-	-	-	-	-
6	$bFaulty$	-	F	F	F	T	T	T	-	-	-	-
Actions		1	2	3	4	1	1	1	1	1	1	1

#	Actions
1	$eArbRequest=cState_1$
2	$eArbRequest=cState_2$
3	$eArbRequest=cState_3$
4	$eArbRequest=cState_4$

(a) Stateflow truth table

Conditions		Result
		$eArbRequest$
$eDrvRequest == cState_1$		$cState_1$
$eDrvRequest == cState_2$	$\neg bFaulty$	$bCmpntUnlocked$ $\neg bCmpntUnlocked$
	$bFaulty$	$cState_2$ $cState_1$
$eDrvRequest == cState_3$	$\neg bFaulty$	$bCmpntUnlocked$ $\neg bCmpntUnlocked$
	$bFaulty$	$cState_3$ $cState_1$
$eDrvRequest == cState_4$	$\neg bFaulty$	$bCmpntUnlocked$ $\neg bCmpntUnlocked$
	$bFaulty$	$cState_4$ $cState_1$

(b) HCT

# SIMPLIFICATION 1

## A. Condition Ordering

- Vertical
  - Move decisions with the most “don’t cares” to upper rows to increase efficiency and speed of evaluation

Conditions			Result
			<i>eArbRequest</i>
<i>eDrvrrRequest</i> == <i>cState</i> <sub>1</sub>			<i>cState</i> <sub>1</sub>
<i>eDrvrrRequest</i> == <i>cState</i> <sub>2</sub>	¬ <i>bFaulty</i>	<i>bCmpntUnlocked</i>	<i>cState</i> <sub>2</sub>
		¬ <i>bCmpntUnlocked</i>	<i>cState</i> <sub>1</sub>
<i>eDrvrrRequest</i> == <i>cState</i> <sub>3</sub>	¬ <i>bFaulty</i>	<i>bFaulty</i>	<i>cState</i> <sub>1</sub>
		<i>bCmpntUnlocked</i>	<i>cState</i> <sub>3</sub>
		¬ <i>bCmpntUnlocked</i>	<i>cState</i> <sub>1</sub>
<i>eDrvrrRequest</i> == <i>cState</i> <sub>4</sub>	¬ <i>bFaulty</i>	<i>bFaulty</i>	<i>cState</i> <sub>1</sub>
		<i>bCmpntUnlocked</i>	<i>cState</i> <sub>4</sub>
		¬ <i>bCmpntUnlocked</i>	<i>cState</i> <sub>1</sub>
		<i>bFaulty</i>	<i>cState</i> <sub>1</sub>

(a) Pre-simplification

Conditions			Result
			<i>eArbRequest</i>
<i>eDrvrrRequest</i> == <i>cState</i> <sub>1</sub>			<i>cState</i> <sub>1</sub>
<i>eDrvrrRequest</i> == <i>cState</i> <sub>2</sub>	¬ <i>bFaulty</i>	<i>bFaulty</i>	<i>cState</i> <sub>1</sub>
		<i>bCmpntUnlocked</i>	<i>cState</i> <sub>2</sub>
<i>eDrvrrRequest</i> == <i>cState</i> <sub>3</sub>	¬ <i>bFaulty</i>	¬ <i>bCmpntUnlocked</i>	<i>cState</i> <sub>1</sub>
		<i>bFaulty</i>	<i>cState</i> <sub>1</sub>
		<i>bCmpntUnlocked</i>	<i>cState</i> <sub>3</sub>
<i>eDrvrrRequest</i> == <i>cState</i> <sub>4</sub>	¬ <i>bFaulty</i>	¬ <i>bCmpntUnlocked</i>	<i>cState</i> <sub>1</sub>
		<i>bFaulty</i>	<i>cState</i> <sub>1</sub>
		<i>bCmpntUnlocked</i>	<i>cState</i> <sub>4</sub>
		¬ <i>bCmpntUnlocked</i>	<i>cState</i> <sub>1</sub>

(b) Vertical reordering of *bFaulty* for consistency

A. Condition Ordering, *Continued*

- Horizontal
  - Nest conditions to minimize evaluation
  - Visual means of representing the dominance of conditions

Conditions		Result	
		<i>eArbRequest</i>	
<i>eDvrRequest</i> == <i>cState</i> <sub>1</sub>		<i>cState</i> <sub>1</sub>	
<i>eDvrRequest</i> == <i>cState</i> <sub>2</sub>	<i>bFaulty</i>	<i>cState</i> <sub>1</sub>	
	¬ <i>bFaulty</i>	<i>bCmpntUnlocked</i>	<i>cState</i> <sub>2</sub>
		¬ <i>bCmpntUnlocked</i>	<i>cState</i> <sub>1</sub>
<i>eDvrRequest</i> == <i>cState</i> <sub>3</sub>	<i>bFaulty</i>	<i>cState</i> <sub>1</sub>	
	¬ <i>bFaulty</i>	<i>bCmpntUnlocked</i>	<i>cState</i> <sub>3</sub>
		¬ <i>bCmpntUnlocked</i>	<i>cState</i> <sub>1</sub>
<i>eDvrRequest</i> == <i>cState</i> <sub>4</sub>	<i>bFaulty</i>	<i>cState</i> <sub>1</sub>	
	¬ <i>bFaulty</i>	<i>bCmpntUnlocked</i>	<i>cState</i> <sub>4</sub>
		¬ <i>bCmpntUnlocked</i>	<i>cState</i> <sub>1</sub>

(a) Pre-simplification

Conditions		Result	
		<i>eArbRequest</i>	
<i>bFaulty</i>		<i>cState</i> <sub>1</sub>	
¬ <i>bFaulty</i>	<i>eDvrRequest</i> == <i>cState</i> <sub>1</sub>	<i>bCmpntUnlocked</i>	<i>cState</i> <sub>1</sub>
		¬ <i>bCmpntUnlocked</i>	<i>cState</i> <sub>1</sub>
	<i>eDvrRequest</i> == <i>cState</i> <sub>2</sub>	<i>bCmpntUnlocked</i>	<i>cState</i> <sub>2</sub>
		¬ <i>bCmpntUnlocked</i>	<i>cState</i> <sub>1</sub>
	<i>eDvrRequest</i> == <i>cState</i> <sub>3</sub>	<i>bCmpntUnlocked</i>	<i>cState</i> <sub>3</sub>
		¬ <i>bCmpntUnlocked</i>	<i>cState</i> <sub>1</sub>
	<i>eDvrRequest</i> == <i>cState</i> <sub>4</sub>	<i>bCmpntUnlocked</i>	<i>cState</i> <sub>4</sub>
		¬ <i>bCmpntUnlocked</i>	<i>cState</i> <sub>1</sub>

(b) Horizontal reordering of *bFaulty* to show dominance

## B. Granted State Simplification

- Particularly useful for systems which arbitrate operational modes
- A condition check is not required when the condition's value is granted and passed through
- The mode variable can be directly placed in the result column

Conditions			Result
<i>bFaulty</i>			<i>eArbRequest</i>
<i>¬bFaulty</i>	<i>eDvrRequest == cState<sub>1</sub></i>	<i>bCmpntUnlocked</i>	<i>cState<sub>1</sub></i>
		<i>¬bCmpntUnlocked</i>	<i>cState<sub>1</sub></i>
	<i>eDvrRequest == cState<sub>2</sub></i>	<i>bCmpntUnlocked</i>	<i>cState<sub>2</sub></i>
		<i>¬bCmpntUnlocked</i>	<i>cState<sub>1</sub></i>
	<i>eDvrRequest == cState<sub>3</sub></i>	<i>bCmpntUnlocked</i>	<i>cState<sub>3</sub></i>
		<i>¬bCmpntUnlocked</i>	<i>cState<sub>1</sub></i>
	<i>eDvrRequest == cState<sub>4</sub></i>	<i>bCmpntUnlocked</i>	<i>cState<sub>4</sub></i>
		<i>¬bCmpntUnlocked</i>	<i>cState<sub>1</sub></i>

(a) Pre-simplification

Conditions			Result
<i>bFaulty</i>			<i>eArbRequest</i>
<i>¬bFaulty</i>	<i>bCmpntUnlocked</i>	<i>eDvrRequest == cState<sub>1</sub></i>	<i>eDvrRequest</i>
		<i>eDvrRequest == cState<sub>2</sub></i>	<i>cState<sub>1</sub></i>
	<i>¬bCmpntUnlocked</i>	<i>eDvrRequest == cState<sub>3</sub></i>	<i>cState<sub>1</sub></i>
		<i>eDvrRequest == cState<sub>4</sub></i>	<i>cState<sub>1</sub></i>

(b) Granted state simplification of *eDvrRequest*

## C. Removal of “Don’t Care” Conditions

- When a condition does not affect the outcome of a decision, it is treated as a “don’t care”
- Identify multiple instances of the **same output** in the results
  - If the paths are the same except for one condition, and can be combined to cover the range of the condition’s type

Conditions			Result
			<i>eArbRequest</i>
<i>bFaulty</i>			<i>cState<sub>1</sub></i>
<i>bCmpntUnlocked</i>			<i>eDrvRRequest</i>
<i>¬bFaulty</i>	<i>¬bCmpntUnlocked</i>	<i>eDrvRRequest == cState<sub>1</sub></i>	<i>cState<sub>1</sub></i>
		<i>eDrvRRequest == cState<sub>2</sub></i>	<i>cState<sub>1</sub></i>
		<i>eDrvRRequest == cState<sub>3</sub></i>	<i>cState<sub>1</sub></i>
		<i>eDrvRRequest == cState<sub>4</sub></i>	<i>cState<sub>1</sub></i>

(a) Pre-simplification

Conditions		Result
		<i>eArbRequest</i>
<i>bFaulty</i>		<i>cState<sub>1</sub></i>
<i>¬bFaulty</i>	<i>bCmpntUnlocked</i>	<i>eDrvRRequest</i>
	<i>¬bCmpntUnlocked</i>	<i>cState<sub>1</sub></i>

(b) Simplifying *eDrvRRequest* to a “don’t care”

### D. Grouping

- A **subset** of rows which lead to the same output can be grouped
- Used when removing mode-centric conditions in their entirety is not achievable, or unnecessary

### E. Compound Simplification

- **Expand** already simplified rows to enable further table simplification through the use of the newly introduced rows
- Useful when altering an existing table to display a design in a specific manner that corresponds to a requirement

1. Remove tabular expression formatting
2. Transpose
3. Construct condition section
4. Construct action section

Conditions		Result
		<i>eArbRequest</i>
<i>bFaulty</i>		<i>cState<sub>1</sub></i>
<i>¬bFaulty</i>	<i>bCmpntUnlocked</i>	<i>eDrvrRequest</i>
	<i>¬bCmpntUnlocked</i>	<i>cState<sub>1</sub></i>

(a) HCT

		Decisions		
#	Conditions	D <sub>1</sub>	D <sub>2</sub>	D <sub>3</sub>
1	<i>bFaulty</i>	T	F	F
2	<i>bCmpntUnlocked</i>	-	T	F
Actions		1	2	1

#	Actions
1	<i>eArbRequest=cState<sub>1</sub></i>
2	<i>eArbRequest=eDrvrRequest</i>

(b) Stateflow truth table

- **Formal proof** of equivalence between original and refactored tabular expressions with *Prototype Verification System* (PVS)
  - The equivalence between steps is easy to see
  - Verifying equivalence between other intermediate steps is also possible
- Methodology applied to the remaining tables of the subsystem
- Refactored tables replaced original tables in the model



## CASE STUDY 1: RESULTS

- Compare original & refactored designs w.r.t. testing and complexity
- *Simulink Design Verifier* (SDV) was used

	Original	Refactored
Tests	7	9
Test Steps	97	48
Test Time (s)	18	7.8
Number of Objectives	1016	371
Objectives Satisfied	797 (78%)	311 (84%)
Objectives Proven Unsatisfiable	219 (22%)	60 (16%)
Cyclomatic Complexity	274	107

**Table 2:** Comparison of test suite generation and complexity

	Original			Refactored		
	Satisfied	Total	Percentage	Satisfied	Total	Percentage
Condition	368	452	81%	110	140	79%
Decision to	112	112	100%	95	95	100%
MC/DC	141	226	62%	44	70	63%

**Table 3:** Comparison of test coverage

## CASE STUDY 1: RESULTS

- Can be used directly in **documentation**
- HCTs are generally more readable
- Requirements presented more evidently and thus are more traceable

Conditions		Result
	$bFaulty$	$eArbRequest$
	$bFaulty$	$cState_1$
$\neg bFaulty$	$bCmpntUnlocked$	$eDrvrRequest$
	$\neg bCmpntUnlocked$	$cState_1$

**Requirement:** “remain in  $cState_1$  when there are no faults, but the component is locked”

2 Stateflow truth tables + 1 calibration matrix

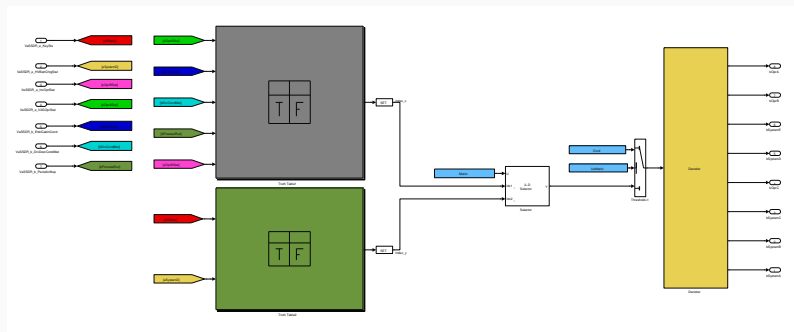


Figure 9: Subsystem for determining overall system status



	Original	Refactored
Tests	23	6
Test Steps	1214	24
Test Time (s)	100	3.6
Number of Objectives	1954	498
Objectives Satisfied	1591 (82%)	445 (89%)
Objectives Proven Unsatisfiable	202 (10%)	53 (10%)
Objectives Undecided	161 (8%)	0
Cyclomatic Complexity	935	248

**Table 4:** Comparison of test suite generation and complexity

	Original			Refactored		
	Satisfied	Total	Percentage	Satisfied	Total	Percentage
Condition	1309	1672	78%	363	418	87%
Decision	297	300	99%	84	84	100%
MC/DC	473	836	57%	154	209	74%

**Table 5:** Comparison of test coverage

## Conclusions

- Proposed a methodology for the refactoring of complex tabular designs
  - \* Shown to increase testability and decrease complexity
- Applied to two industrial models
- **Refactored designs incorporated into production code**

## Future Work

- Simulink lacks model refactoring tools
- Tool support and automation